



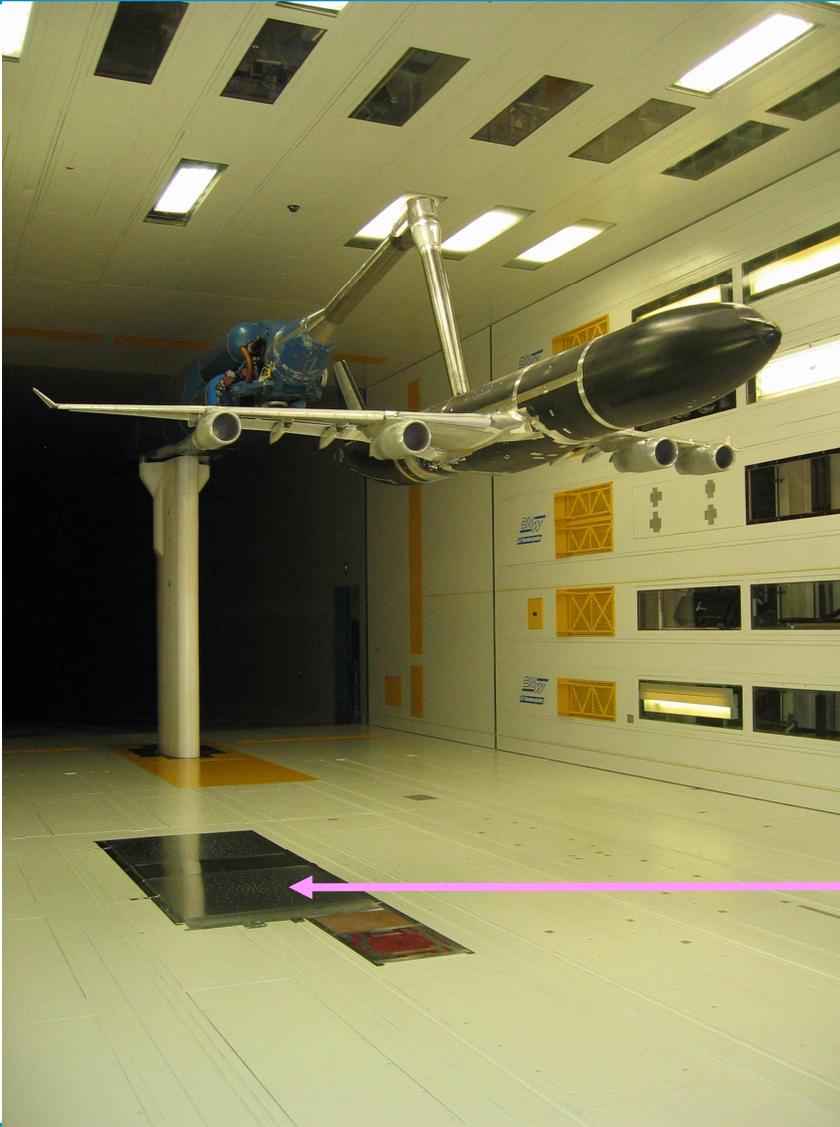
*Dedicated to innovation in aerospace*



## **CLEAN Based on Spatial Source Coherence**

*Pieter Sijtsma*

# Acoustic array measurements in closed wind tunnel test section

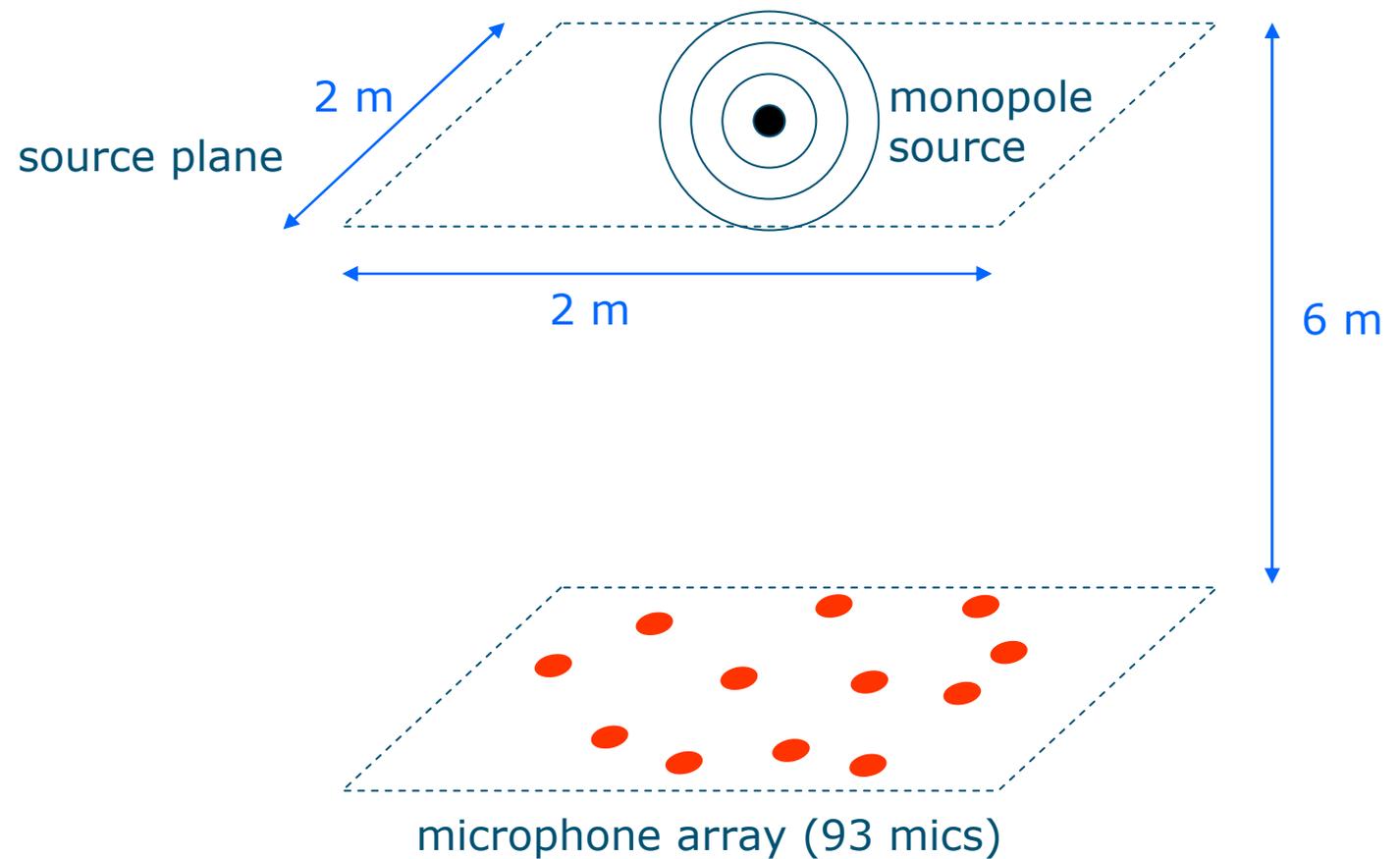


**Airbus A340 model in  
DNW-LLF 8x6 m<sup>2</sup> closed  
test section (AWIATOR)**

wall mounted array

# CLEAN-CLASSIC (1)

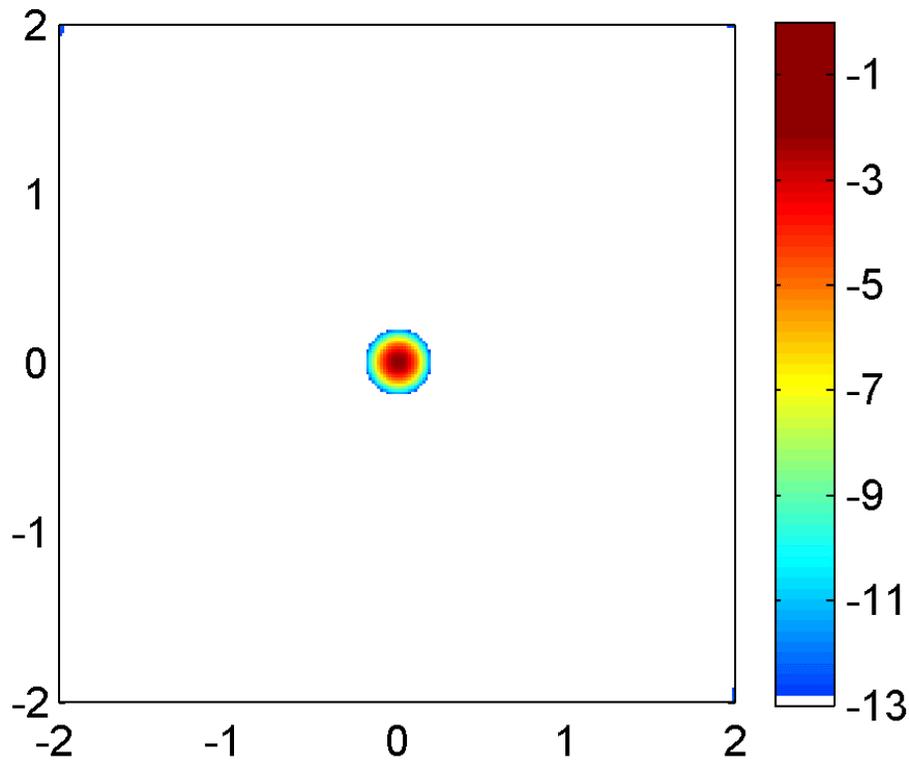
## Array simulations



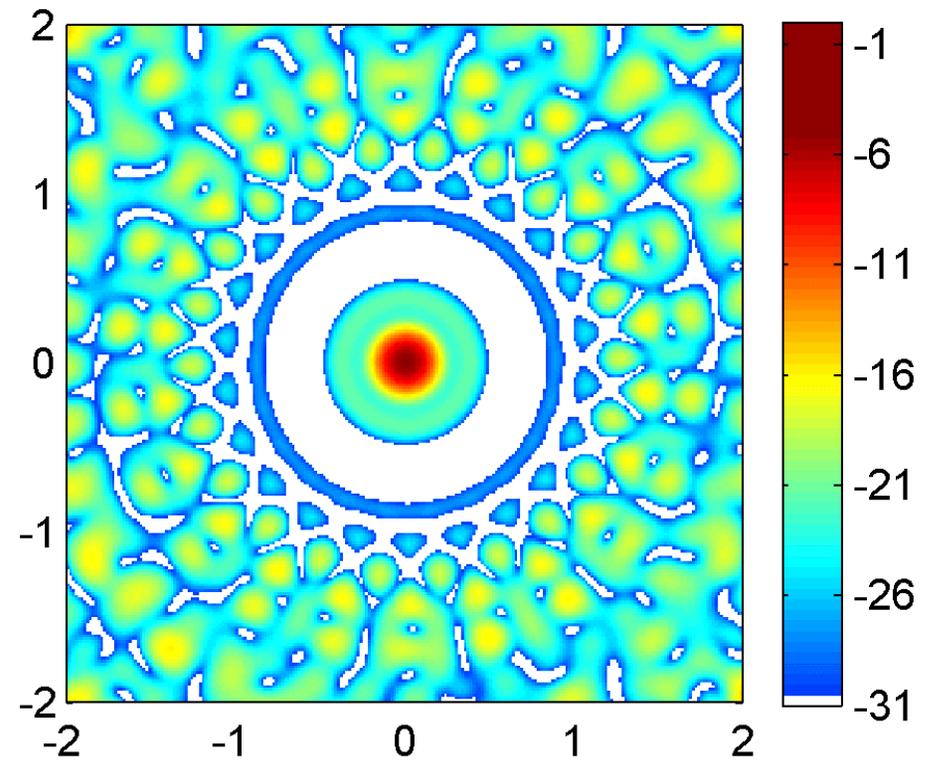
# CLEAN-CLASSIC (2)

## Conventional Beamforming

source plot at 13 dB range



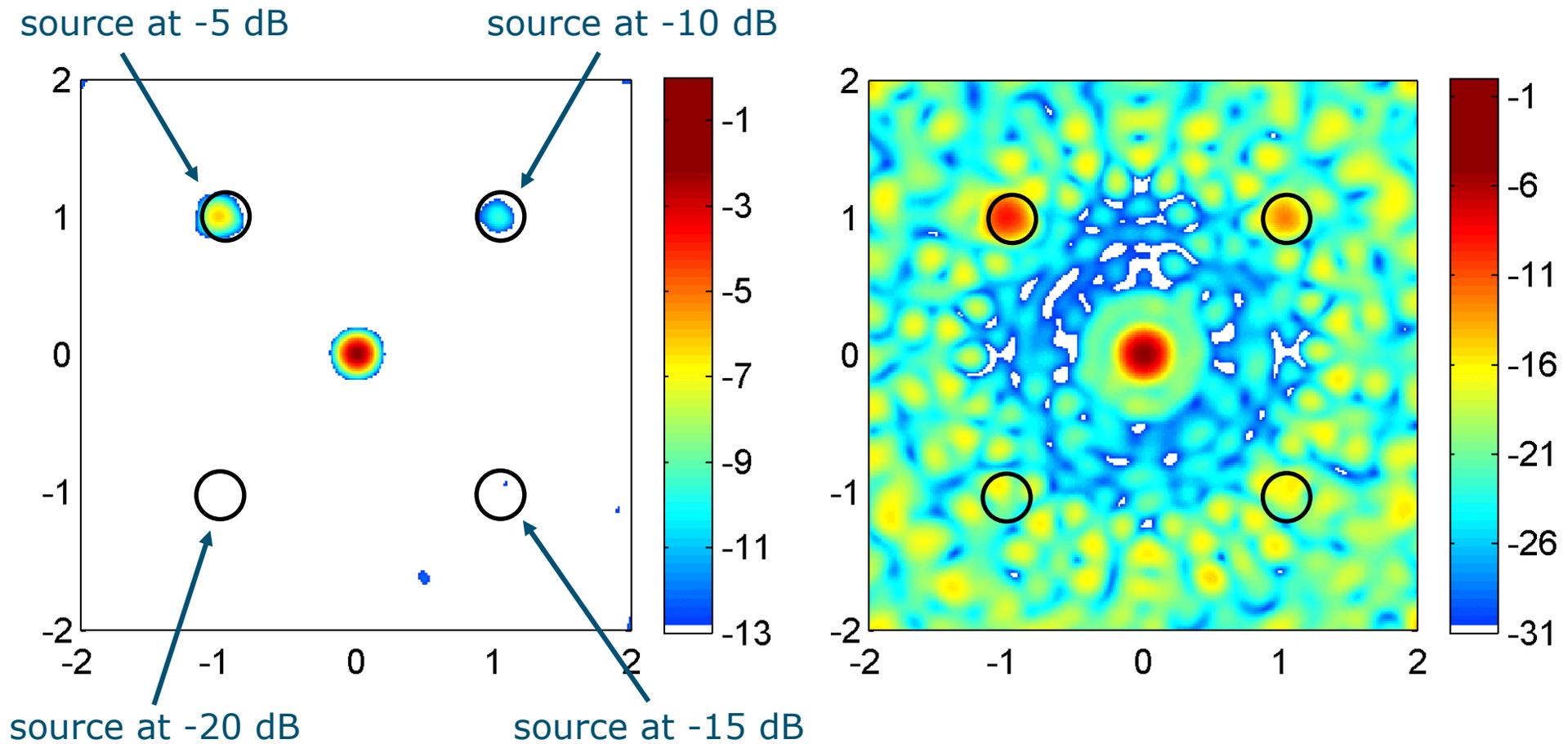
source plot at 31 dB range



"Point Spread Function"

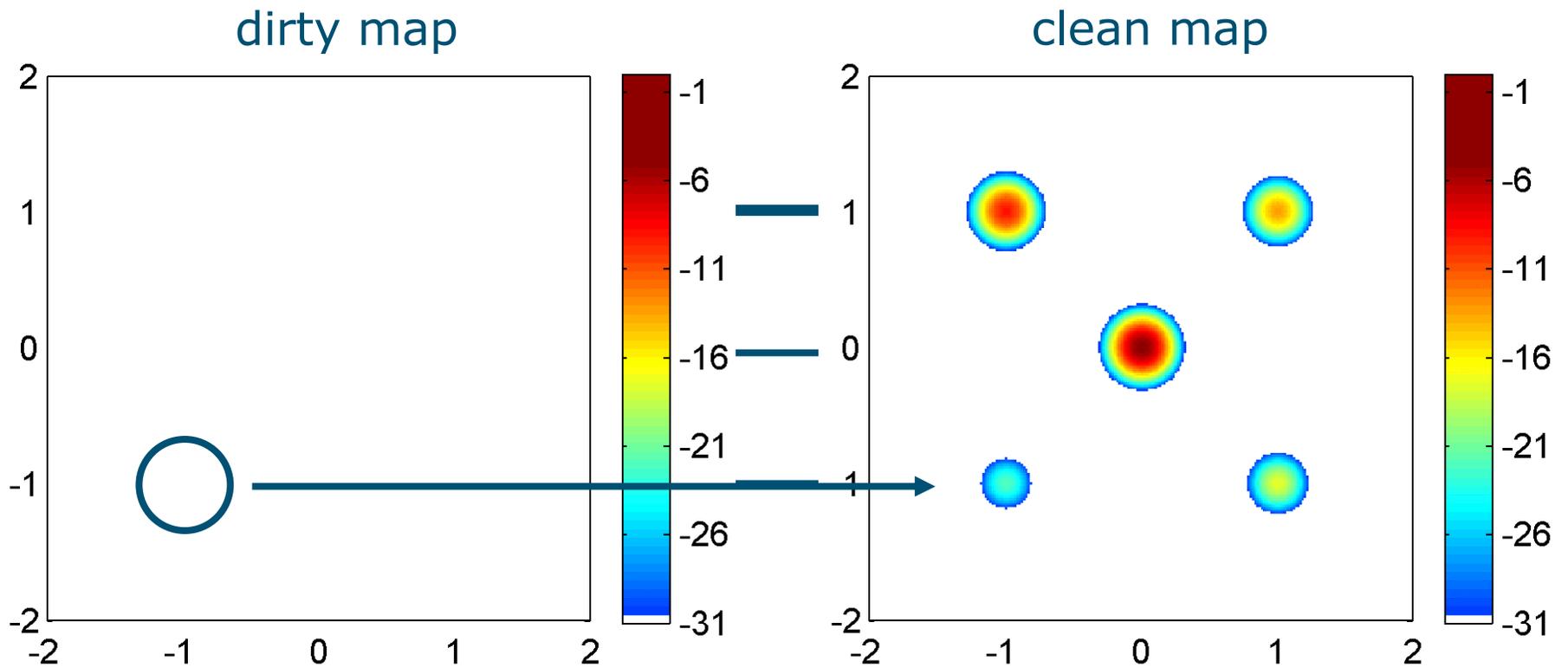
# CLEAN-CLASSIC (3)

## Secondary sources added



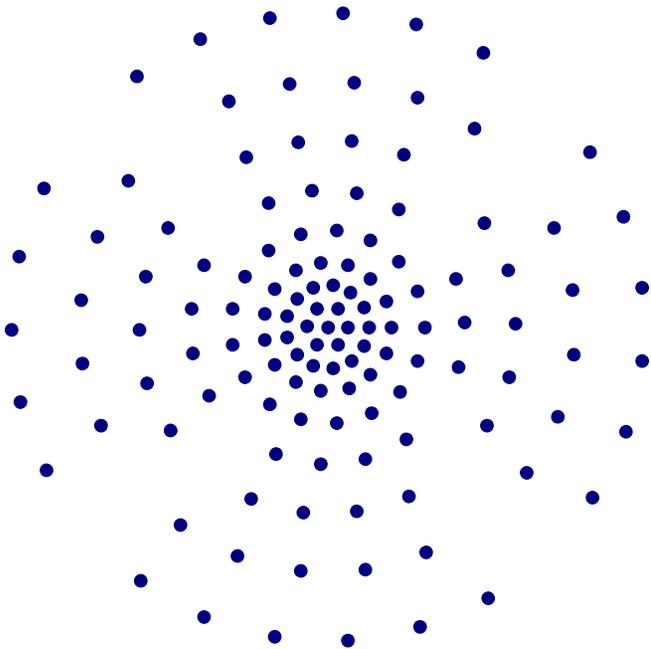
# CLEAN-CLASSIC (4)

## Successively remove Point Spread Functions



## A340 scale model (1)

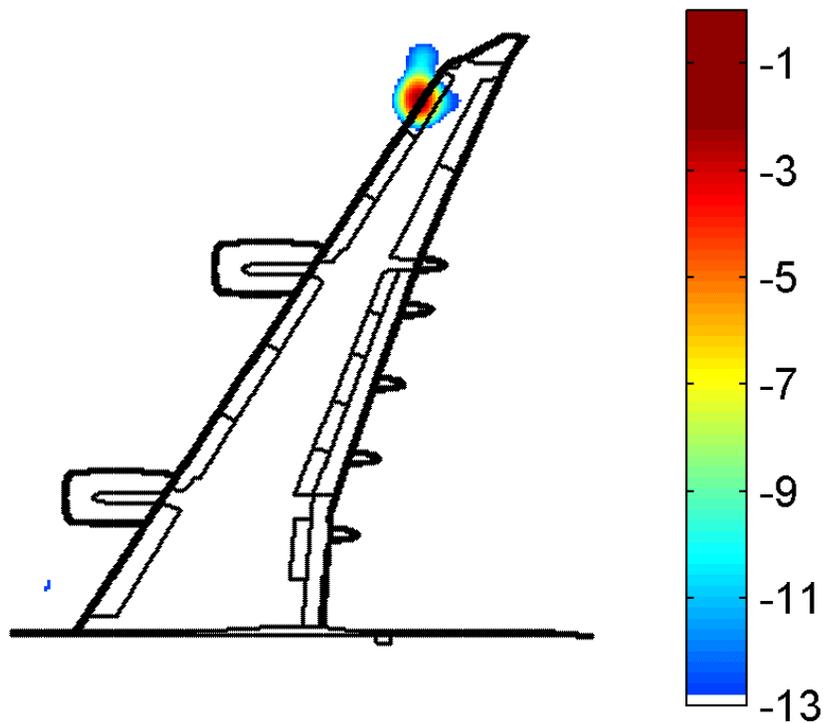
- DNW-LLF 8x6 m<sup>2</sup> closed test section
- Scale = 1:10.6
- Flush mounted floor array
- 128 microphones



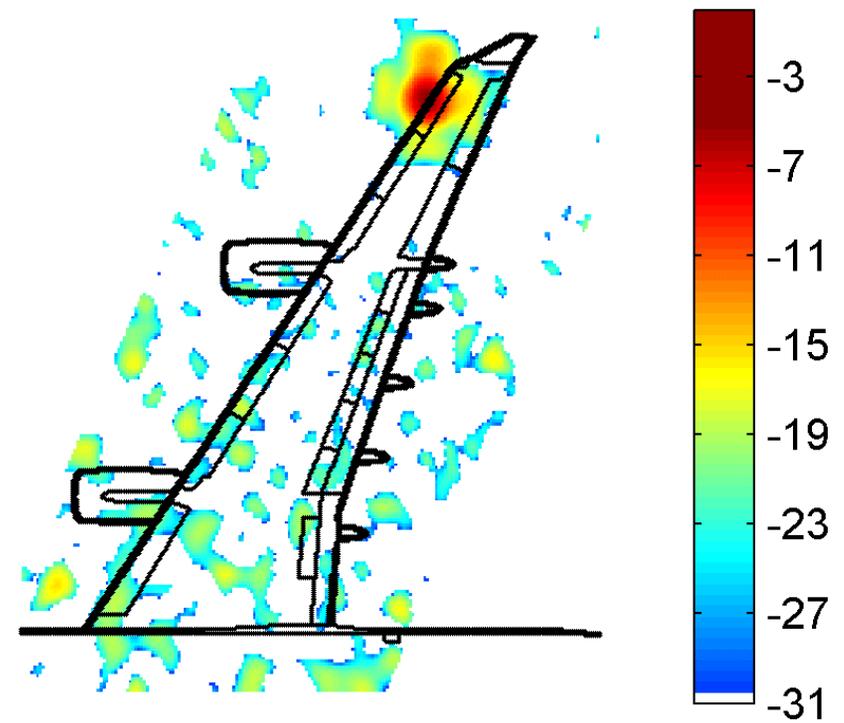
# A340 scale model (2)

## dominant slat noise source at 12360 Hz

source plot at 13 dB range



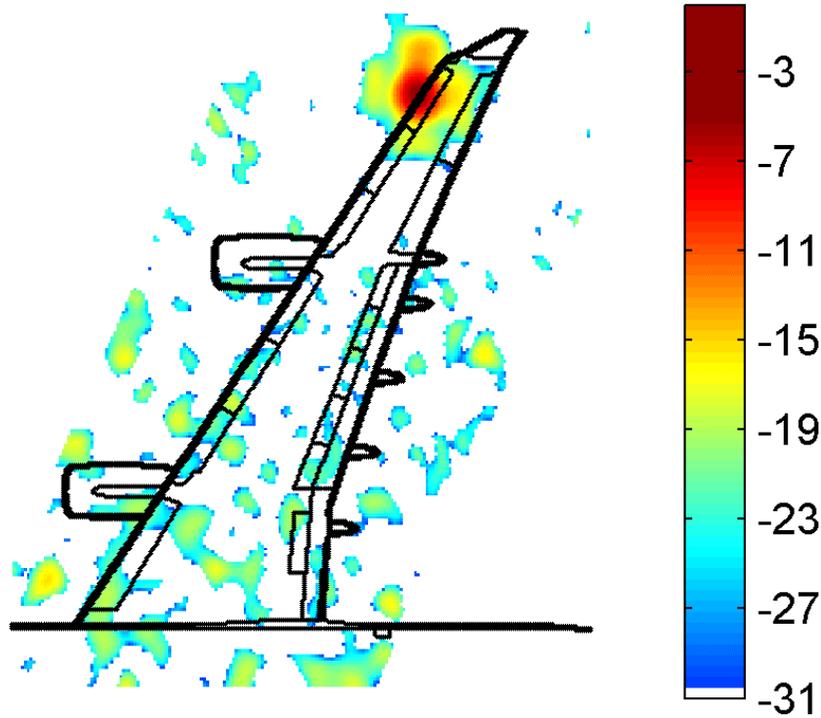
source plot at 31 dB range



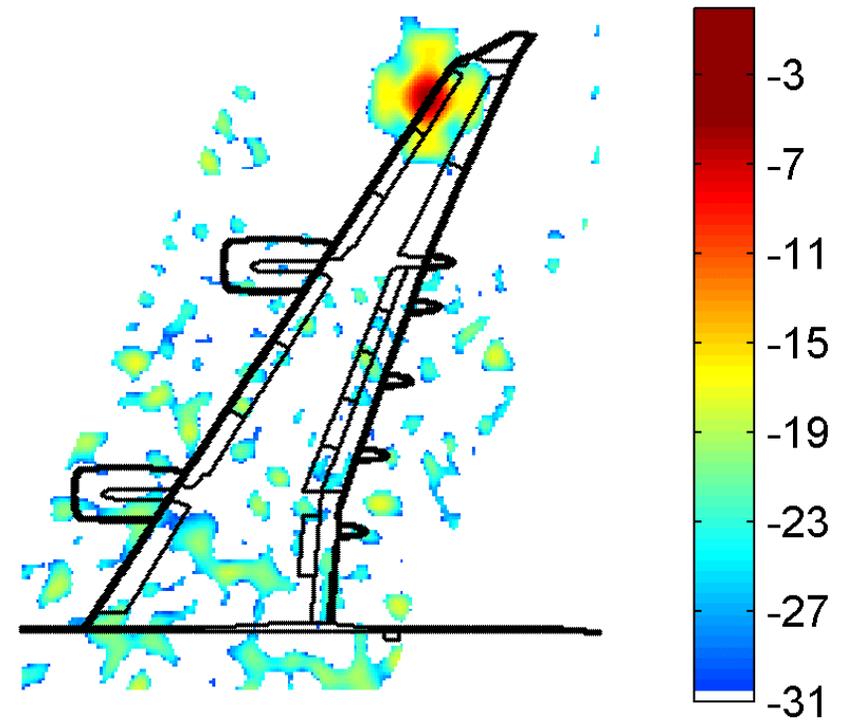
# A340 scale model (3)

## Similarity with Point Spread Function

measurement



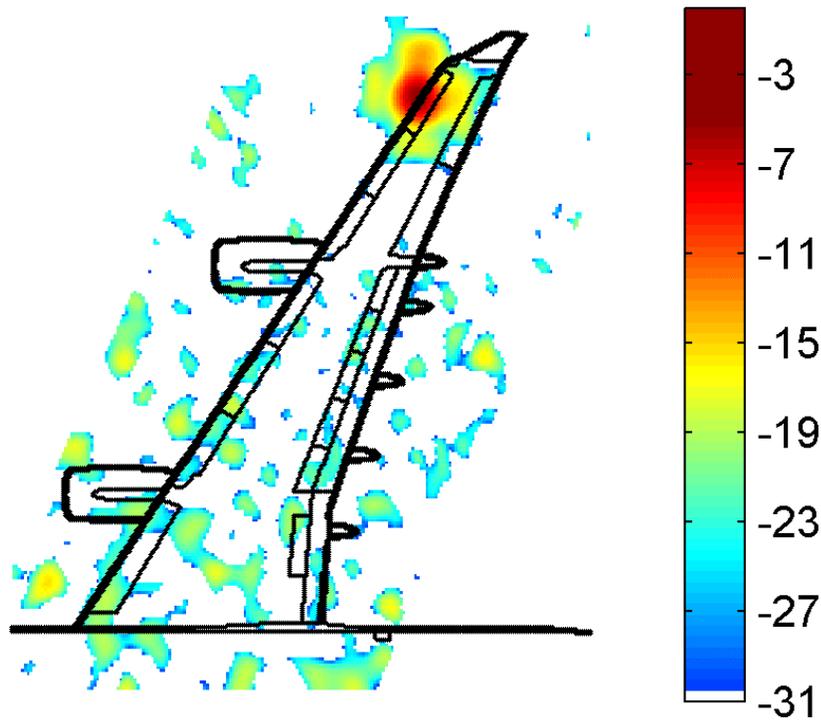
Point Spread Function



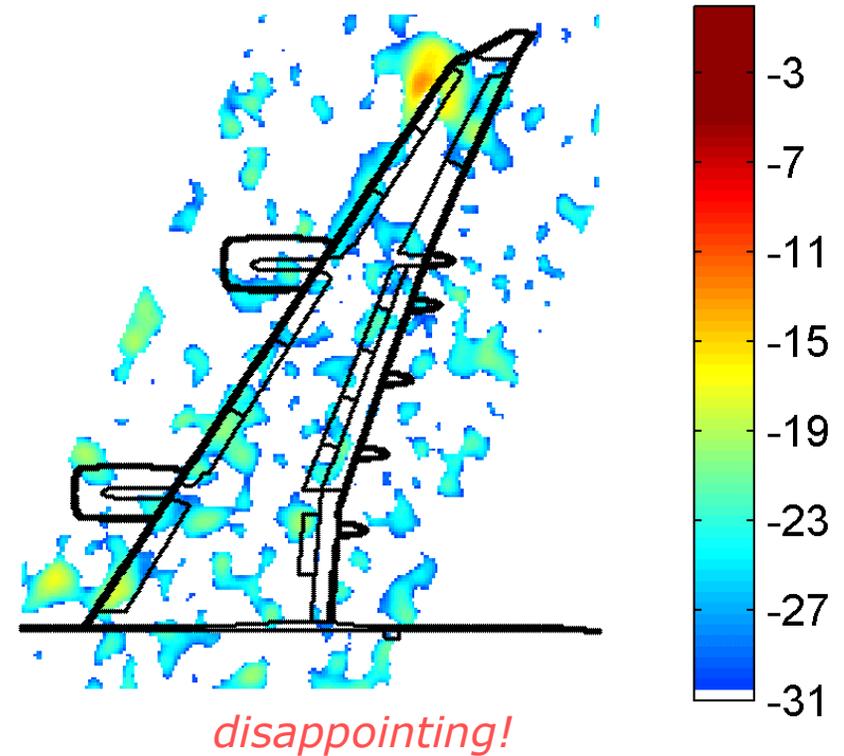
# A340 scale model (4)

## Application of CLEAN – first step

Conventional Beamforming



PSF subtracted



## A340 scale model (5)

- **Beam pattern of dominant source  $\neq$  Point Spread Function**
- **Possible reasons:**
  - source is not a point source
  - source does not have uniform directivity
  - error in height of source plane
  - error in flow Mach number
  - flow is not uniform
  - errors in microphone sensitivity
  - loss of coherence
- **Motivation for CLEAN based on spatial source coherence (CLEAN-SC)**

# Spatial source coherence (1)

## Conventional definition of coherence

Consider microphone signals  $p_n$  (frequency domain)

$$\text{Auto-powers: } C_{nn} = \langle |p_n|^2 \rangle$$

$$\text{Cross-powers: } C_{mn} = \langle p_m p_n^* \rangle$$

$$\text{Coherence: } \gamma_{mn}^2 = \frac{|C_{mn}|^2}{C_{mm} C_{nn}}$$

Suppose  $p_n$  and  $p_m$  have constant amplitude and fixed phase difference:

$$\rightarrow \gamma_{mn}^2 = 1$$

$$\text{Otherwise: } 0 \leq \gamma_{mn}^2 < 1$$

## Spatial source coherence (2)

### Beamforming summary

Source auto-power in scan point  $\vec{\xi}_j$  :  $A_{jj} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_j$

$\mathbf{C}$  = matrix of cross-powers (Cross-Spectral Matrix)

$\mathbf{w}_j$  = weight vector associated with  $\vec{\xi}_j$

property:  $A_{jj} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_j = 1$ , when  $\mathbf{C} = \mathbf{g}_j \mathbf{g}_j^*$

$\mathbf{g}_j$  = steering vector

(microphone pressures due to theoretical point source in  $\vec{\xi}_j$ )

## Spatial source coherence (3)

### Source coherence

Source auto-power in  $\vec{\xi}$  :  $A_{jj} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_j$

Source cross-power between  $\vec{\xi}_j$  and  $\vec{\xi}_k$  :  $A_{jk} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_k$

Source coherence:  $\Gamma_{jk}^2 = \frac{|A_{jk}|^2}{A_{jj} A_{kk}} = \frac{|\mathbf{w}_j^* \mathbf{C} \mathbf{w}_k|^2}{(\mathbf{w}_j^* \mathbf{C} \mathbf{w}_j)(\mathbf{w}_k^* \mathbf{C} \mathbf{w}_k)}$

## Spatial source coherence (4)

### Single coherent source

Constant amplitude and fixed phase difference:  $\mathbf{C} = \langle \mathbf{p}\mathbf{p}^* \rangle = \mathbf{p}\mathbf{p}^*$

$$\Rightarrow A_{jk} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_k = \mathbf{w}_j^* \mathbf{p} \mathbf{p}^* \mathbf{w}_k = (\mathbf{w}_j^* \mathbf{p})(\mathbf{p}^* \mathbf{w}_k)$$

$$\Gamma_{jk}^2 = \frac{|A_{jk}|^2}{A_{jj}A_{kk}} = \frac{|(\mathbf{w}_j^* \mathbf{p})(\mathbf{p}^* \mathbf{w}_k)|^2}{(\mathbf{w}_j^* \mathbf{p})(\mathbf{p}^* \mathbf{w}_j)(\mathbf{w}_k^* \mathbf{p})(\mathbf{p}^* \mathbf{w}_k)} = 1$$

## Spatial source coherence (5)

### Peaks & side lobes

At peaks and side lobes: array output dominated by single coherent source

$$\Rightarrow A_{jk} \approx \mathbf{w}_j^* \mathbf{p} \mathbf{p}^* \mathbf{w}_k = (\mathbf{w}_j^* \mathbf{p})(\mathbf{p}^* \mathbf{w}_k) \text{ and } \Gamma_{jk}^2 \approx 1$$

# Basics of CLEAN-SC (1)

## General loop

1. Calculate source auto-powers in  $\xi_j$ :  $A_{jj} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_j$
2. Determine peak value  $A_{kk}$
3. Subtract coherent part:  $A_{jj}^{\text{updated}} = A_{jj} (1 - \Gamma_{jk}^2)$

$$= A_{jj} \left( 1 - \frac{|A_{jk}|^2}{A_{jj} A_{kk}} \right) = A_{jj} - \frac{|A_{jk}|^2}{A_{kk}}$$

## Basics of CLEAN-SC (2)

### Small complication

Main diagonal is usually removed from  $\mathbf{C}$

$A_{jj} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_j$  can be negative

$\Gamma_{jk}^2 = \frac{|A_{jk}|^2}{A_{jj} A_{kk}}$  can have all sorts of values (not necessarily  $0 \leq \Gamma_{jk}^2 \leq 1$ )

$A_{jj}^{\text{updated}} = A_{jj} (1 - \Gamma_{jk}^2)$  unstable

# Complication

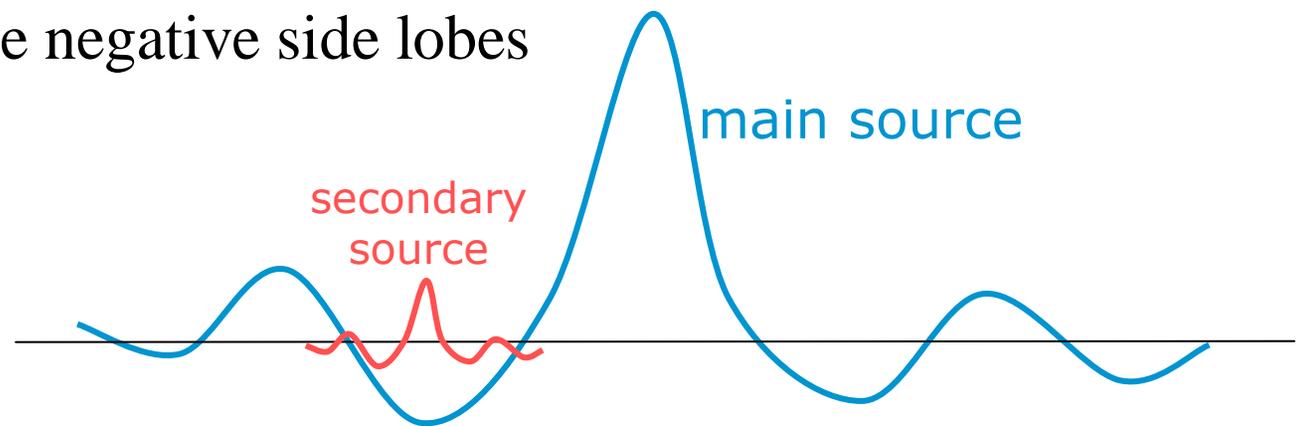
Main diagonal is usually removed from  $\mathbf{C}$

$A_{jj} = \mathbf{w}_j^* \mathbf{C} \mathbf{w}_j$  can have negative values

But  $A_{kk} > 0$  (being a maximum value)

$$A_{jj}^{\text{updated}} = A_{jj} - \frac{|A_{jk}|^2}{A_{kk}} < A_{jj}$$

This does not remove negative side lobes



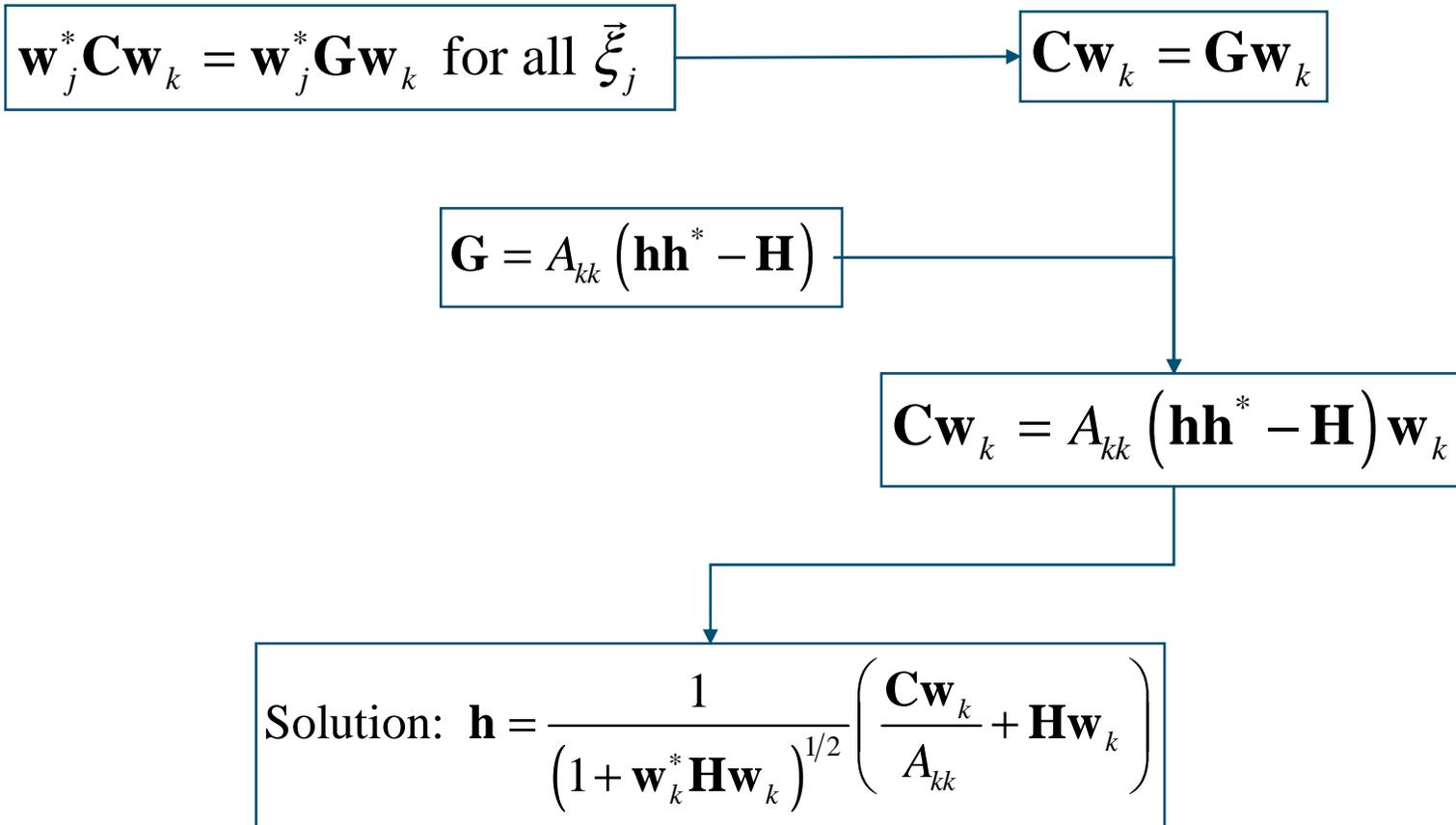
# CLEAN-SC: more general approach

## More general approach required

Subtract "coherent" part:  $A_{jj}^{\text{updated}} = A_{jj} - \mathbf{w}_j^* \mathbf{G} \mathbf{w}_j$

$\left\{ \begin{array}{l} \mathbf{G} \text{ is responsible for the cross-powers with peak source in } \vec{\xi}_k: \\ \mathbf{w}_j^* \mathbf{C} \mathbf{w}_k = \mathbf{w}_j^* \mathbf{G} \mathbf{w}_k \text{ for all } \vec{\xi}_j \\ \mathbf{G} \text{ is induced by a single coherent "source component" } \mathbf{h}: \\ \mathbf{G} = A_{kk} (\mathbf{h} \mathbf{h}^* - \mathbf{H}) \\ (\mathbf{H} \text{ contains the diagonal elements of } \mathbf{h} \mathbf{h}^*) \end{array} \right.$

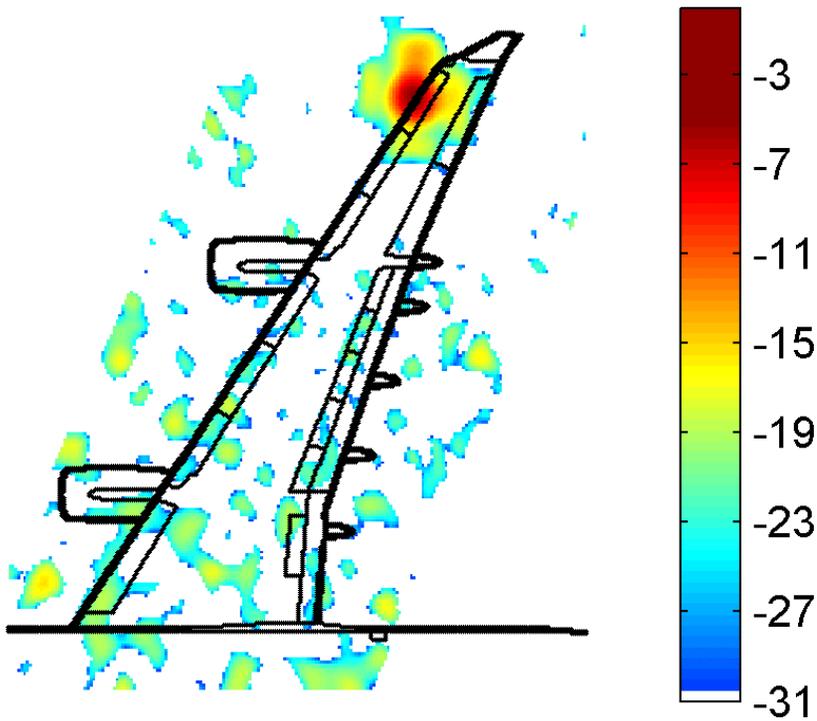
# CLEAN-SC: analysis



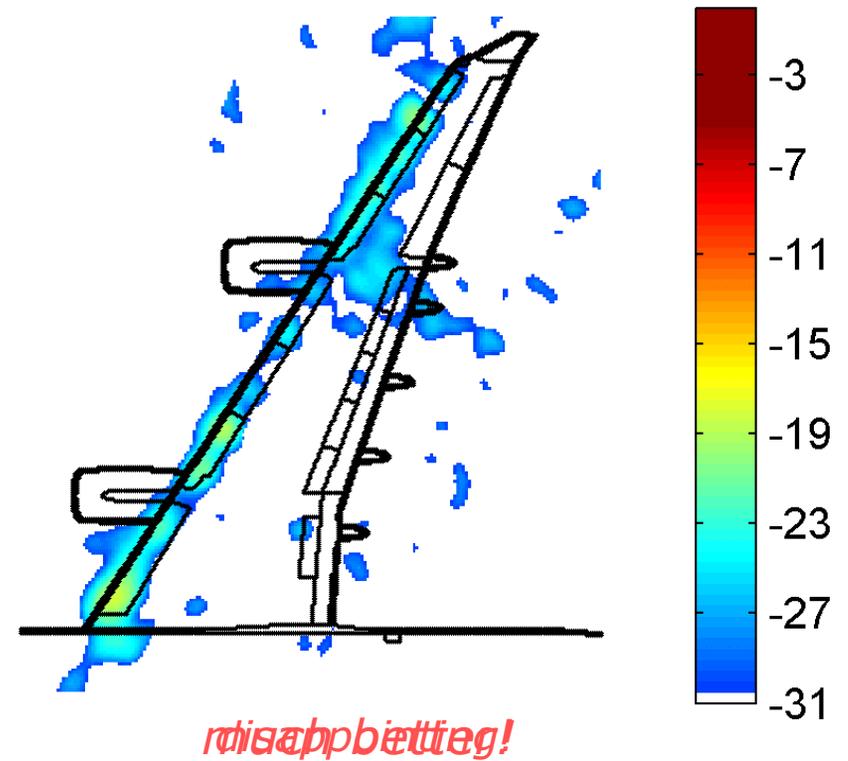
To be solved iteratively, starting with:  $\mathbf{h} = \mathbf{g}_k$  (steering vector)

# CLEAN-SC: main source removal

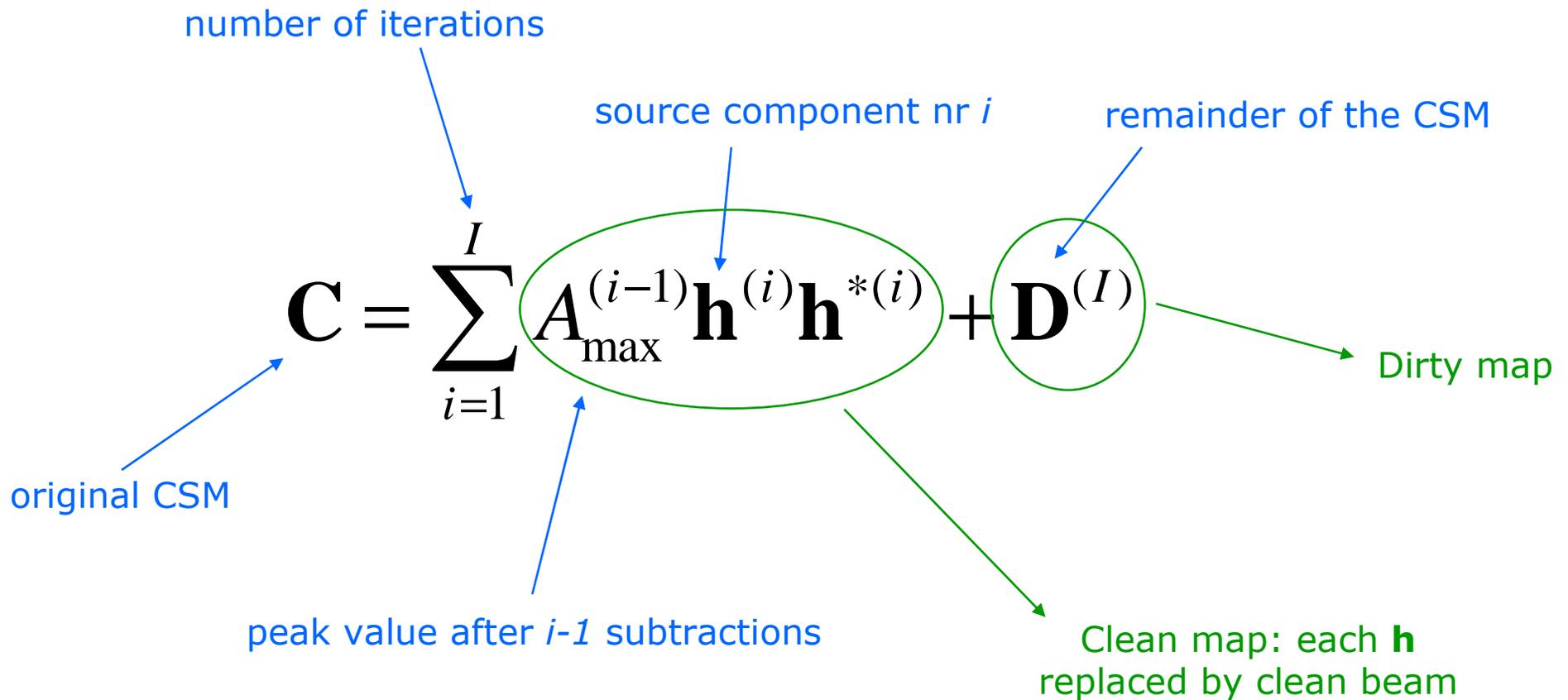
Conventional Beamforming



coherent CSF subtraction



# CLEAN-SC: full deconvolution (1)



## CLEAN-SC: full deconvolution (2)

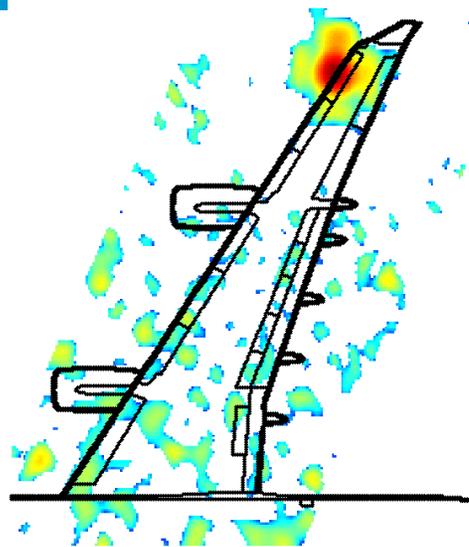
$$\mathbf{C} = \sum_{i=1}^I A_{\max}^{(i-1)} \mathbf{h}^{(i)} \mathbf{h}^{*(i)} + \mathbf{D}^{(I)}$$

Stop criterion:  $\|\mathbf{D}^{(I+1)}\| \geq \|\mathbf{D}^{(I)}\|$

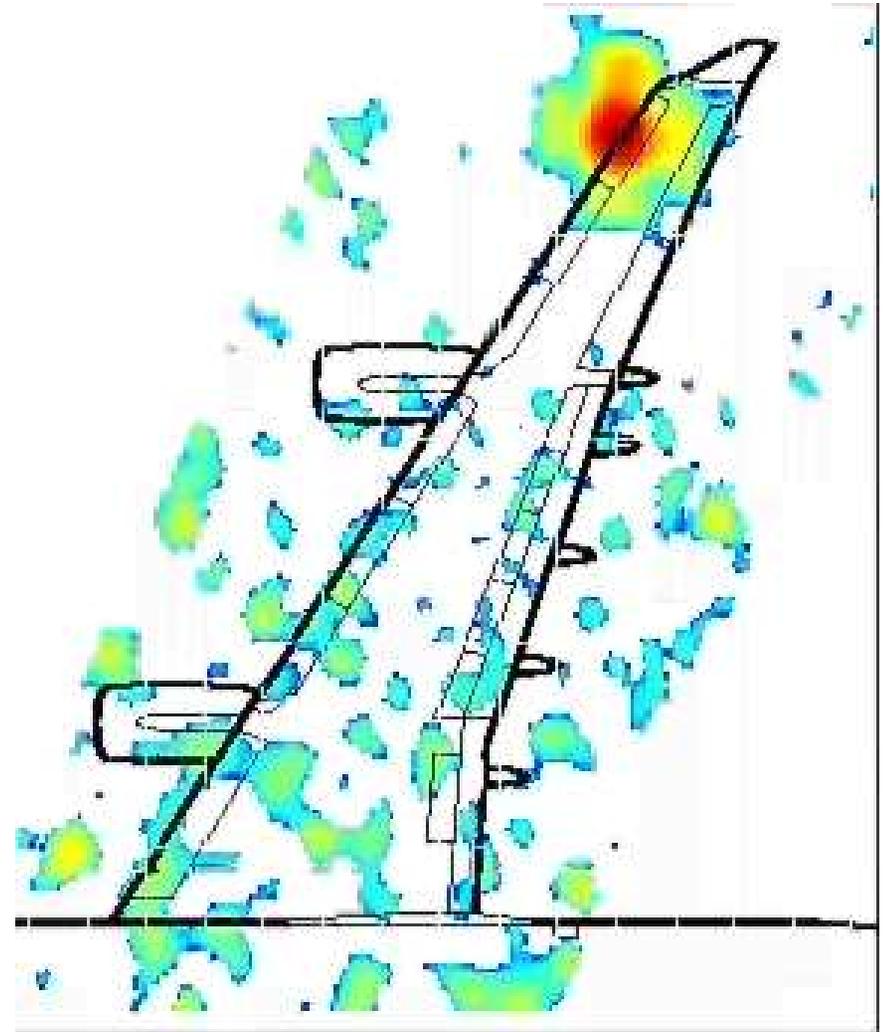
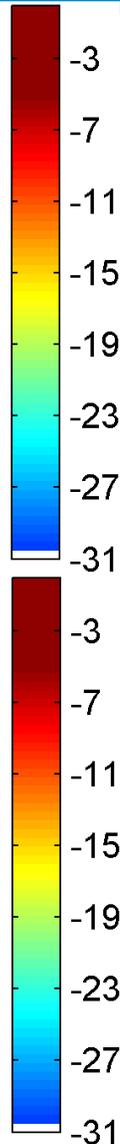
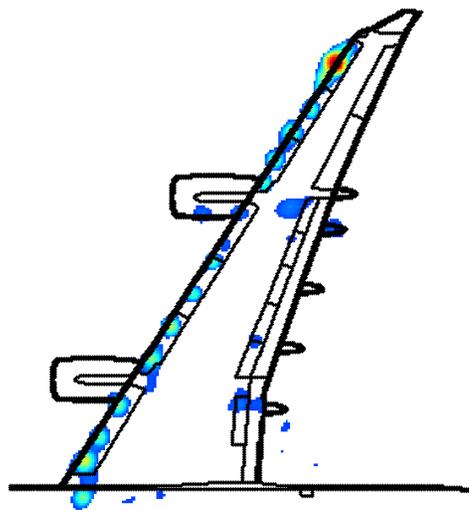
For example:  $\|\mathbf{D}\| = \sum_{m,n} |D_{m,n}|$

# CLEAN-SC: full deconvolution (3)

Conventional Beamforming



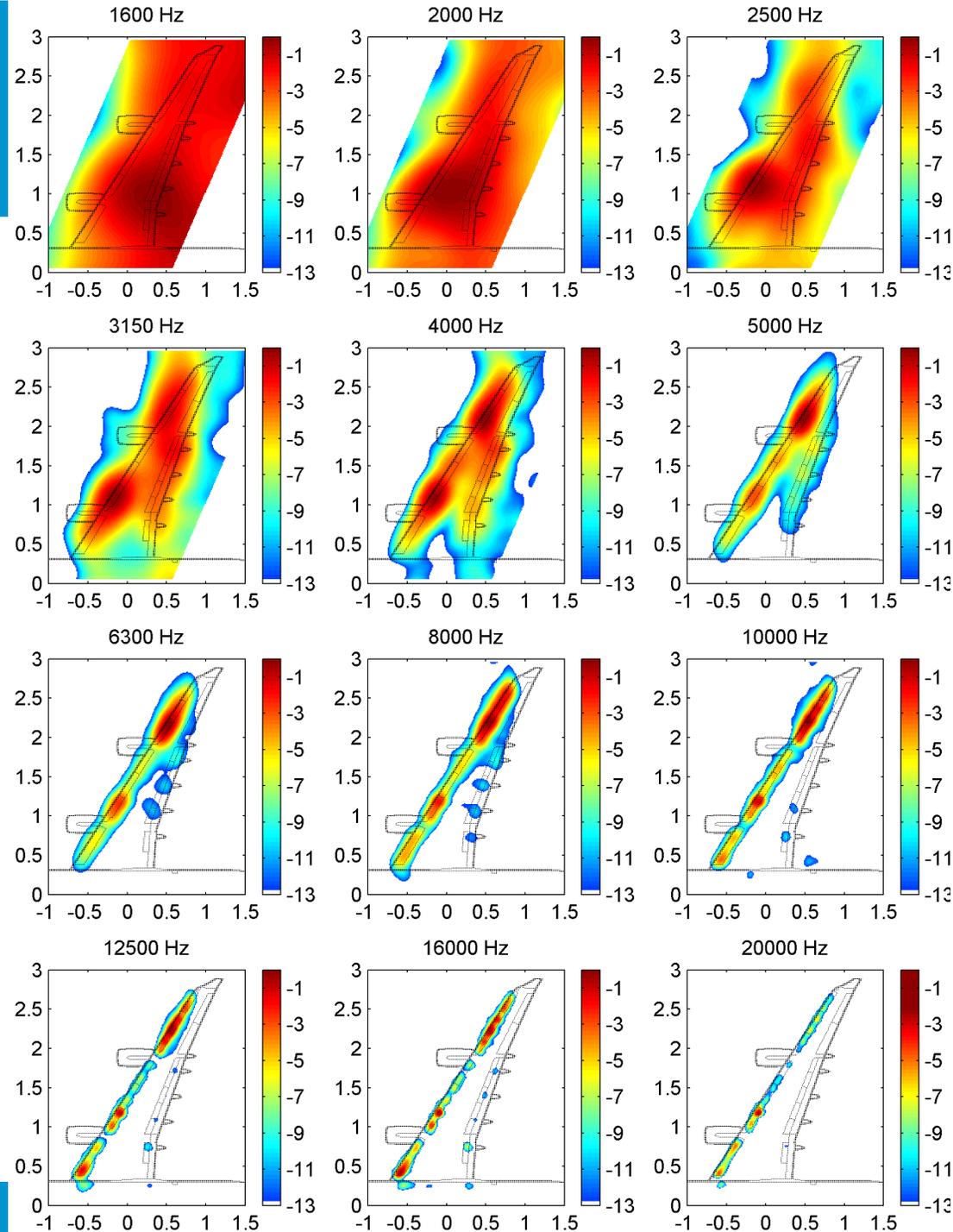
CLEAN-SC



# Example (1)

Typical result at 60 m/s

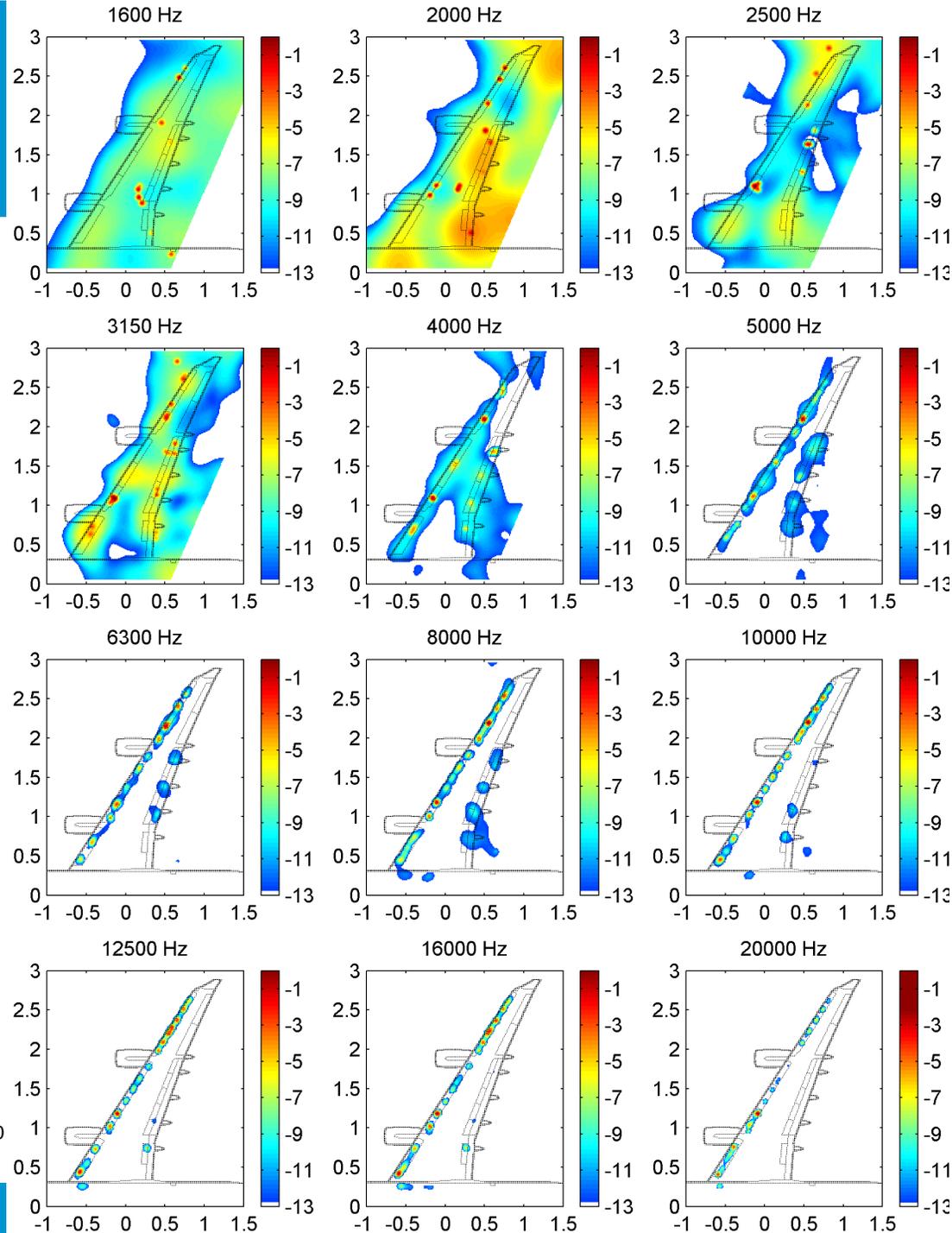
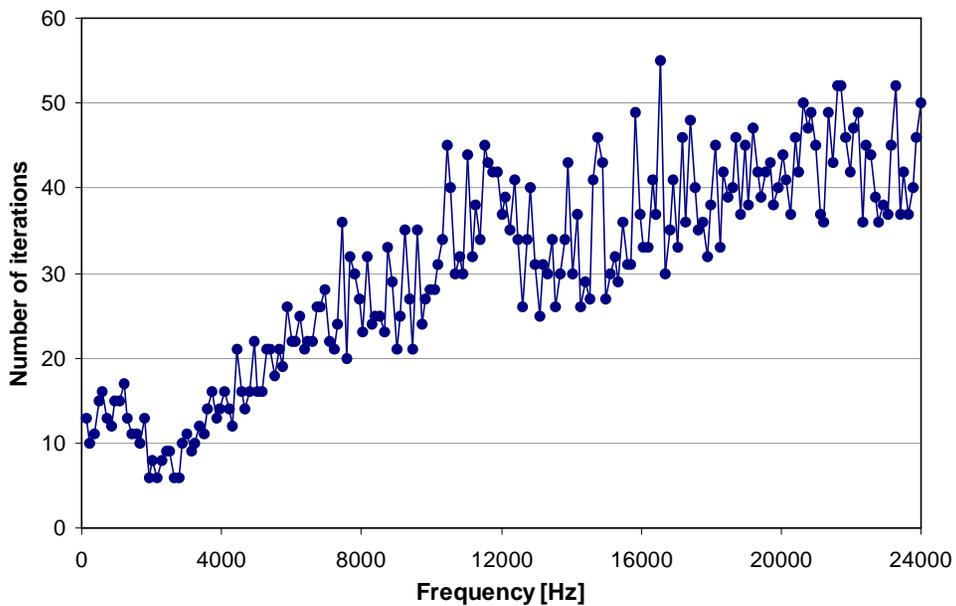
Conventional Beamforming



# Example (2)

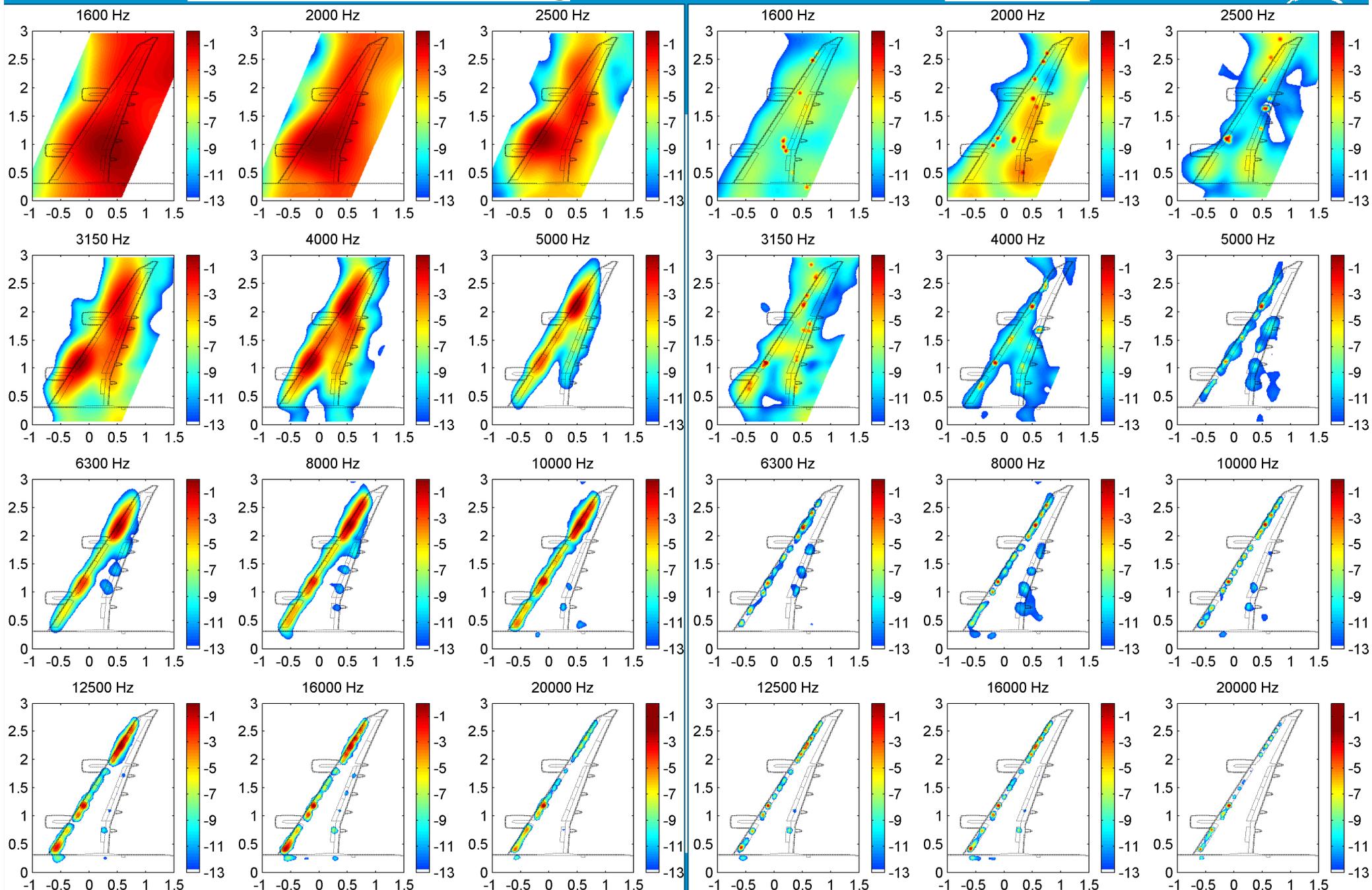
Typical result at 60 m/s

CLEAN-SC



# Conventional Beamforming

# CLEAN-SC



# Features of CLEAN-SC

- **Determination of absolute source contributions**
- **Processing speed**
- **Filtering low frequency wind tunnel noise**

# Absolute source contributions (1)

diagonal removed (due to boundary layer noise)

contains diagonal elements without boundary layer noise

$$\mathbf{C} = \sum_{i=1}^I A_{\max}^{(i-1)} \mathbf{h}^{(i)} \mathbf{h}^{*(i)} + \mathbf{D}^{(I)}$$

trace:

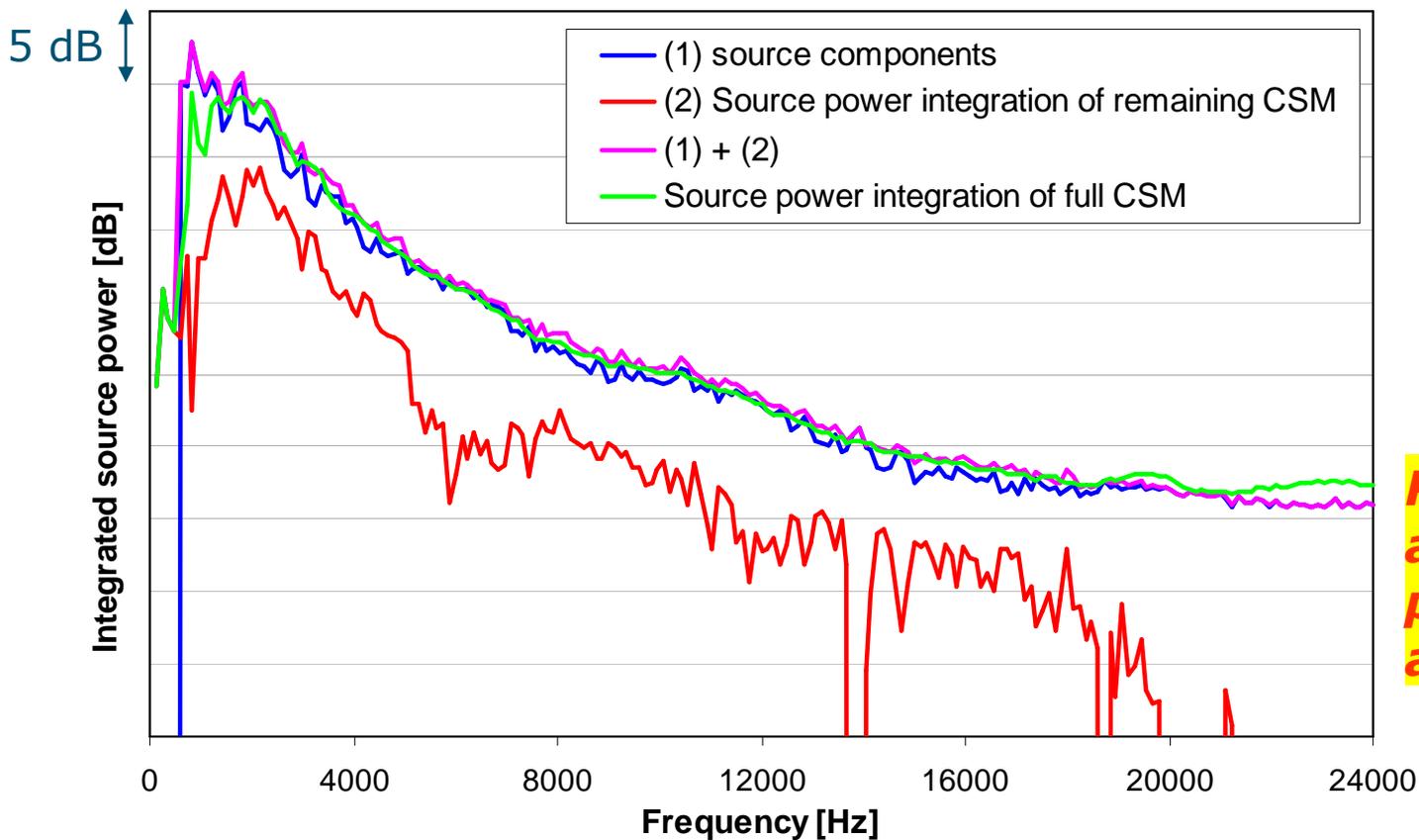
$$\sum_{n=1}^N C_{nn} = \sum_{i=1}^I A_{\max}^{(i-1)} \left\| \mathbf{h}^{(i)} \right\|^2$$

breakdown into source components

# Absolute source contributions (2)

## Integrated results

$$\mathbf{C} = \underbrace{\sum_{i=1}^I A_{\max}^{(i-1)} \mathbf{h}^{(i)} \mathbf{h}^{*(i)}}_{(1)} + \underbrace{\mathbf{D}^{(I)}}_{(2)}$$



**Results of CLEAN-SC and traditional source power integration are almost equal!**

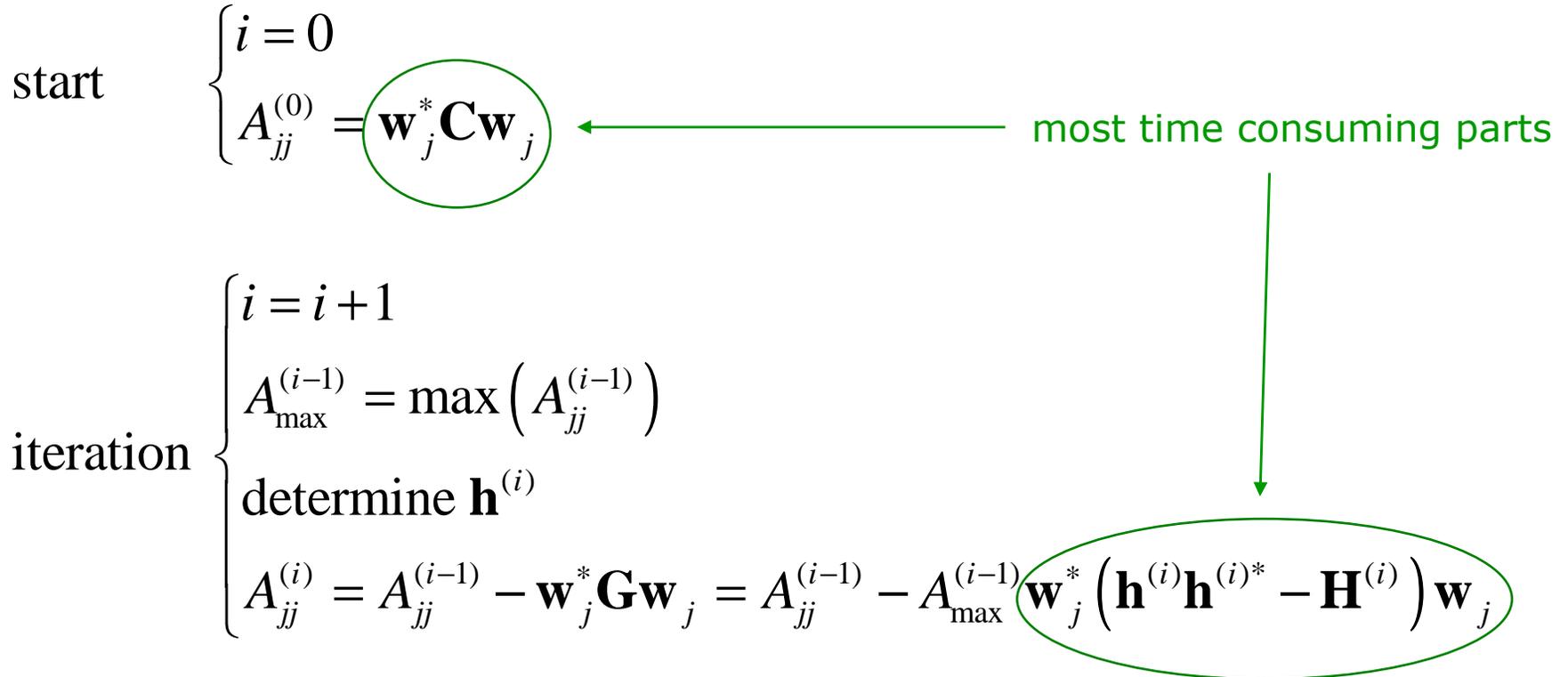
## Absolute source contributions (3)

### Differences with Source Power Integration:

- **Less grid dependence**
  - Grid needs to be such that sources are recognized
  - But no need to have grid points on the exact peaks
- **No integration threshold**
- **Pitfalls:**
  - Side lobes of sources outside the grid are also included
  - Coherent reflections are included as well

# Processing speed (1)

## Summary of algorithm



## Processing speed (2)

start:

$$\mathbf{w}_j^* \mathbf{C} \mathbf{w}_j = \sum_{n=1}^N \sum_{m=1}^M w_{j,n}^* C_{nm} w_{j,m}$$

double summation

iteration steps:

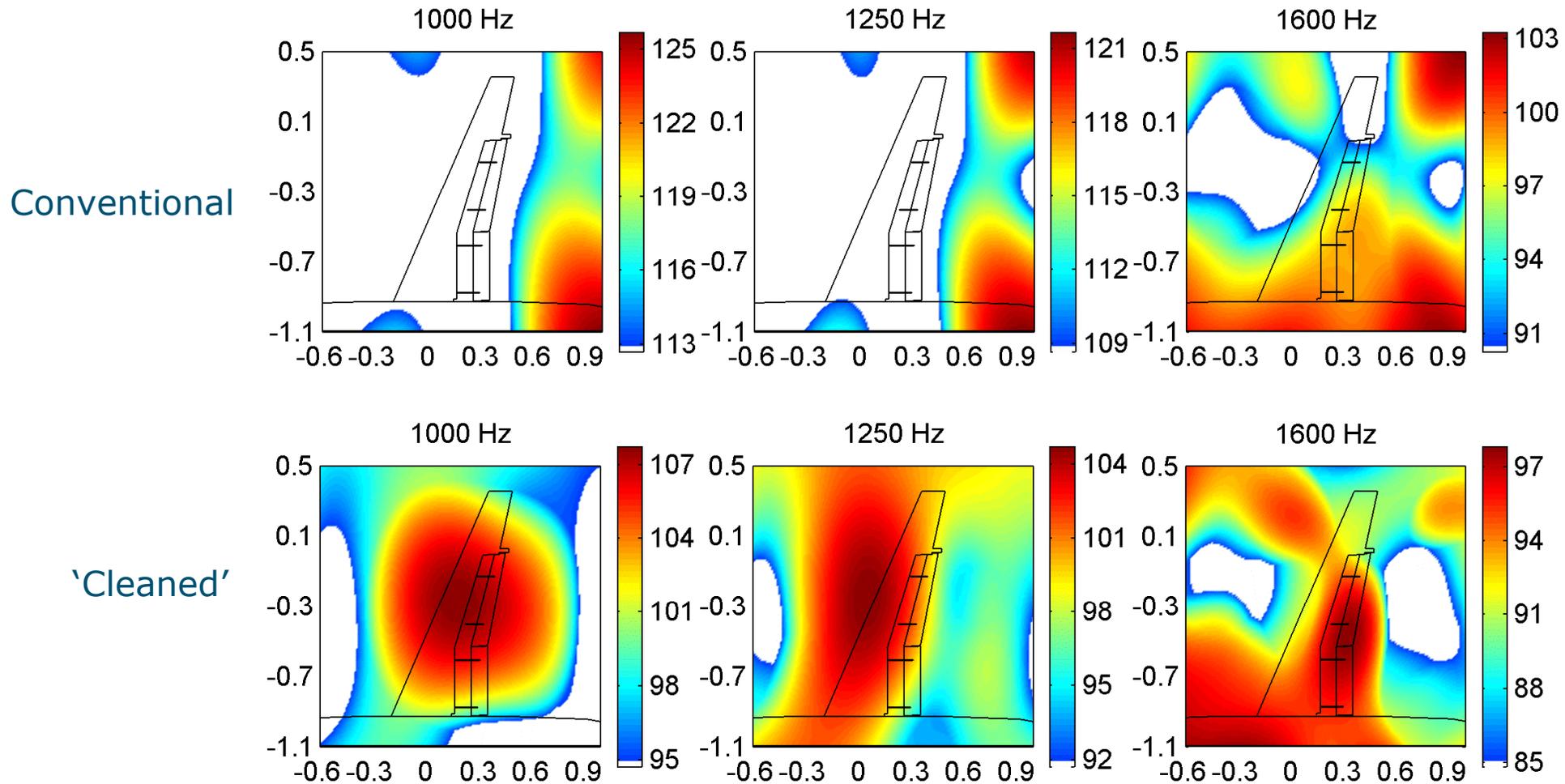
$$\mathbf{w}_j^* \left( \mathbf{h}^{(i)} \mathbf{h}^{(i)*} - \mathbf{H}^{(i)} \right) \mathbf{w}_j = \left| \sum_{n=1}^N w_{j,n}^* h_n^{(i)} \right|^2 - \sum_{n=1}^N \left| w_{j,n}^* h_n^{(i)} \right|^2$$

single summations

- One double summation + many single summations  
 $\approx$  two double summations
- CLEAN-SC about twice as slow as Conventional Beamforming

# Filtering low frequency wind tunnel noise

## Fokker-100 half model in DNW-LST (3x2.25 m<sup>2</sup>)



## Note

- **CLEAN-SC extracts coherent sources from the CSM**
- **When decorrelation occurs: CLEAN-SC will perform less well**
  - Outdoor measurements at large distances from the source
  - Open jet wind tunnel measurements (out-of-flow array)

# Conclusions

- **New deconvolution method: CLEAN-SC**
  - No Point Spread Functions used
  - Works with removed CSM diagonal
  - Counteracts negative side lobes
- **Effective tool for removing dominant sources**
  - also when they are from outside the grid
- **Absolute source powers can be obtained**
  - Good agreement with Source Power Integration
  - No threshold, and not much grid dependence
  - Few pitfalls
- **Relatively short processing time**

## Reference

***International Journal of Aeroacoustics:***

***"CLEAN based on spatial source coherence"***

**volume 6, number 4, 2007, pages 357 – 374**